

An Improved Hierarchical Clustering Algorithm using Feature Reduction Techniques and Clustering Validation Indices

Nitin Soni^{#1}, Prof Abha Choubey^{*2}

^{1,2}*Computer Science and Engineering, Faculty of Engg & Tech, SSGI
Bhilai, India*

Abstract— Number of variables or attributes of any data set effect to a large extent clustering of that particular data. These attributes directly affect the dissimilarity or distance measures thereby effecting accuracy of data. So dimensionality reduction techniques can definitely improve clustering. As clustering is a unsupervised machine learning technique, the validation of results obtained from application of clustering algorithm to a particular data set is a big issue. This paper formulates a new model for data clustering using combination of feature extraction, data clustering algorithm and clustering validity index/indices. The data clustering algorithm used is Agglomerative Hierarchical Clustering Algorithm. The different features reduction techniques used are PCA, CMDS, ISOMAP and HLLC. The clustering validity indices used are Silhouette index, Dunn index, Davies Bouldin Index and Calinski Harbasaz index.

Keywords—Agglomerative Hierarchical Clustering, PCA, CMDS, ISOMAP, HLLC, Silhouette Index, Dunn Index, Davies-Bouldin Index, Calinski Harbasaz Index.

I. INTRODUCTION

Clustering is a process of classifying data tuples into groups called Clusters. The specific characteristics of these groups are not known beforehand. The tuples within a group of cluster are some similar to each other than they are to data instances in other groups. Clustering is an example of Unsupervised Learning. Data clustering is a universal data organization technique with applications in wide variety of fields such as marketing, engineering etc[1]. Different types of clustering algorithms are Hierarchical clustering, Partition clustering, graph clustering, density clustering etc. An important partition based techniques is Agglomerative Clustering Algorithm. This algorithm, considers each data tuple as a cluster. Out of all the clusters, two clusters are selected with minimum distance and are merged. This new cluster replaces the two clusters which have been combined. The above two steps are repeated until all there is only one clustering remaining. Clusters are combined using a distance metric and linkage criteria. Some of the distance metrics used are Euclidean distance, Manhattan distance, Mahalanobis distance etc. Different types of linkage include complete linkage, single linkage, centroid linkage [1]. This paper uses centroid linkage and Euclidean distance.

Feature or Dimensionality Reduction Techniques are used to reduce the number of variables or attributes of the data set. These techniques are linear such as PCA or non-linear such as ISOMAP[2]. The techniques used by this paper for feature reduction are PCA, CMDS, ISOMAP and HLLC.

As clustering is a process of classification where class labels are unknown. So validation of clustering algorithms

is required [3]. There are three types of clustering validity indices:- internal, external and relative indices. Internal Indices measure quality of clustering indices without the use of any external knowledge. External indices compare the clustering algorithm results with class labels of data sets (if known). Relative Indices compare clustering results of different clustering algorithms. This paper uses the following four internal indices:- Davies-Bouldin Index[4], Calinski-Harbasaz Index[5], Dunn's Index[6] and Silhouette Index[7].

Section I of this paper deals with the introduction of concepts used in this paper. Section II deals with Literature Review, Section III deals with Problem Identification, Section IV deals with Methodology, Section V with Datasets used for experiments, Section VI with Experiments and Results, Section VII on improved clustering algorithm Section VIII Conclusion followed by Acknowledgement

II. LITERATURE REVIEW

Impact of dimensionality reduction techniques on data Clustering algorithms has been quantified by researchers in past. In 2004 Chris Ding et al., showed that results of data clustering algorithms can be improved using dimensionality reduction techniques [8]. Seong S. Chaea et al in 2006 showed that Principal Coordinate Analysis (also known as classical multidimensional scaling) is better than Principal Component Analysis in improving data clustering results.[9]. Hai-Dong Meng et al., in 2010 showed that dimensionality reduction techniques had no effect on data clustering algorithms when number of dimensions of data set exceeded 30 [10]. Rajashree Dash et al., in 2010 derived initial centroids of reduced data set obtained by PCA for K-means algorithm and showed improvement in data clustering [11]. In August 2013, S. M. Shaharudin et al., proved that PCA improves data clustering significantly if Tukey's biweight correlation matrix is used instead of Pearson correlation matrix in calculating principal components [12].

Olatz Arbelaitz et al., in 2012, have compared the efficiency of 30 different clustering validity indices [13].

III. PROBLEM IDENTIFICATION

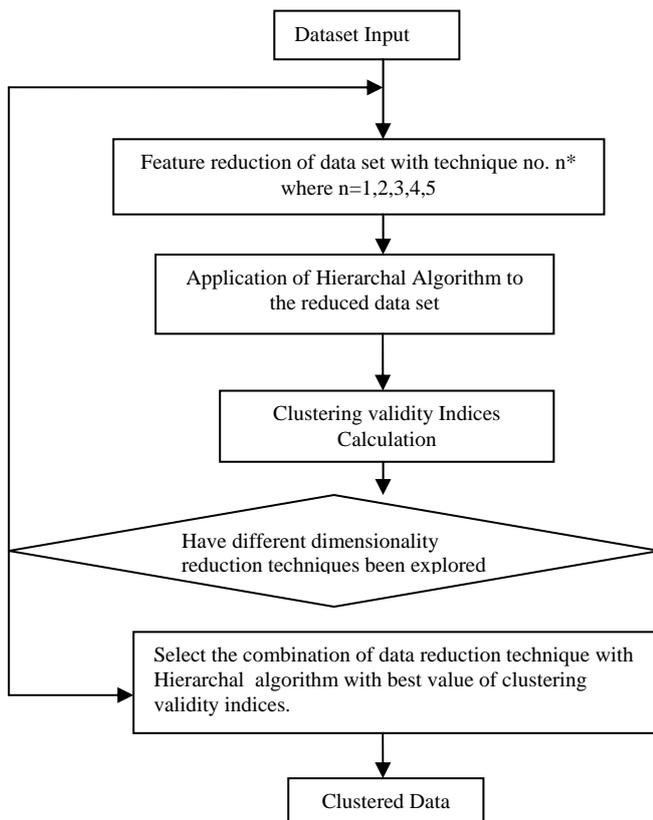
Large number of attributes or dimensions of any particular data set create problems in data clustering. First problem is that efficiency of distance measures such as Euclidean Distance become meaningless. Second problem is data

visualization. Also linear dimensionality reduction techniques have been proven to be ineffective in improving data clustering results when number of dimensions of data set are more than 30 [10].

The large number of clustering validity indices has compounded the problem of data clustering. Different clustering validity indices give different results and at times it is very difficult to choose the clustering validity index for proper validation [13].

IV METHODOLOGY

As shown in the figure, there are two important steps in the proposed model. In the first important step, dimensions of the data set are reduced using different dimensionality reduction techniques. The techniques used are PCA, CMDS, ISOMAP and HLLE. After this step the data is clustered using Hierarchical Clustering Algorithm. In the next step the clustering is validated using different clustering validity indices. In the last step the different clustering validity indices obtained from combination of dimensionality reduction techniques and hierarchical clustering algorithms have compared. In the end, a combination of data reduction technique, hierarchical clustering algorithm and clustering validity index has been proposed. In all, a total of 20 experiments have been conducted before final model has been proposed. The figure 1 shows the methodology used.



*When n=1: No data Reduction, n=2: PCA, n=3: CMDS, n=4: ISOMAP, n=5 HLLE.

FIGURE NO.1 METHODOLOGY

V. DATASET FOR EXPERIMENTS

The dataset used for experiment is Libras Movement Data Set from UCI Machine Learning Repository [14]. This data set has 360 tuples, 90 attributes and 15 clusters.

VI. EXPERIMENTS AND RESULTS

The impact of dimensionality reduction techniques on k-medoids clustering algorithm is shown by studying variation on clustering validity index with respect to number of partitions k. If a clustering validity index for a particular dimensionality reduction techniques accurately predicts the number of partition, that particular feature reduction method and clustering validity index is considered to be effective. In each case the database taken is Libras-Movement database. To conduct experiments, packages from MATLAB and R software are used.

VIA. CHANGES IN SILHOUETTE INDEX

The value of silhouette index ranges from -1 to +1. A value of +1 implies that any data instance assigned to any particular cluster is similar to other instances in that particular cluster and a value of -1 indicates dissimilarity [7]. In figures 2 to 6 shown below depict values of silhouette indices when different dimensionality reduction techniques are used and also when no dimensionality reduction is done. In each figure horizontal axis depicts number of partitions and vertical axis depicts Silhouette index.

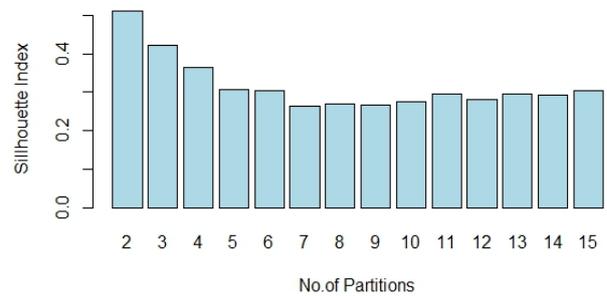


FIGURE NO.2 CHANGES IN SILHOUETTE INDEX WHEN NO DIMENSIONALITY REDUCTION TECHNIQUE IS EMPLOYED

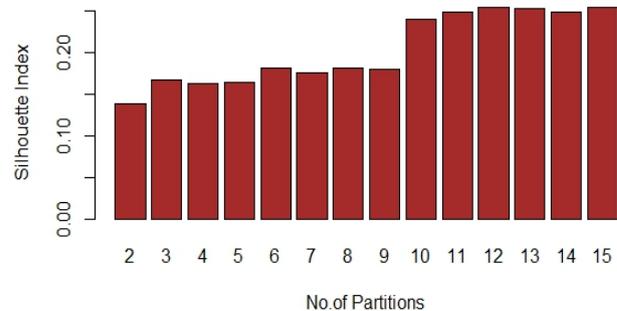


FIGURE NO.3 CHANGES IN SILHOUETTE INDEX WHEN PCA IS EMPLOYED

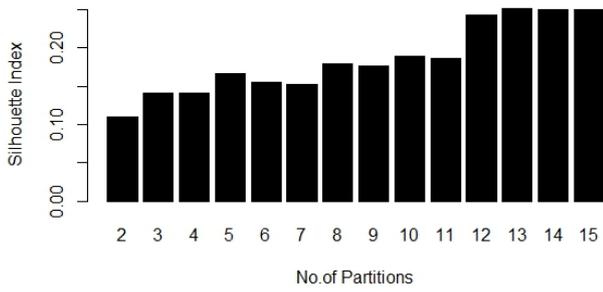


FIGURE NO.4 CHANGES IN SILHOUETTE INDEX WHEN CMDS IS EMPLOYED

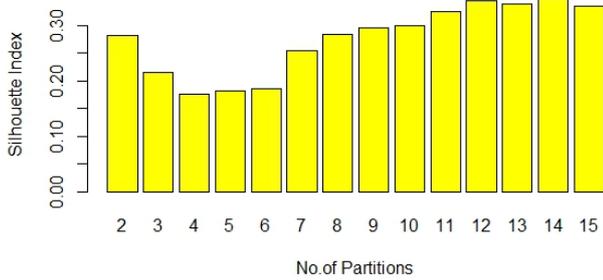


FIGURE NO.5 CHANGES IN SILHOUETTE INDEX WHEN ISOMAP IS USED.

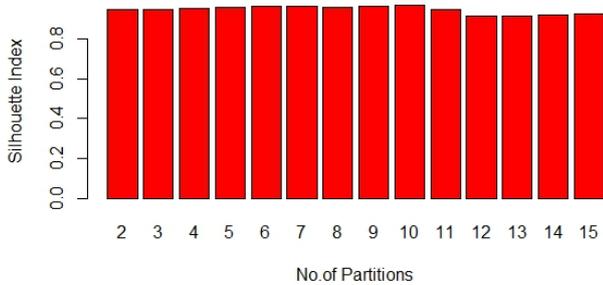


FIGURE NO.6 CHANGES IN SILHOUETTE INDEX WHEN ISOMAP IS USED

It is evident from above bar graphs, the silhouette index range when HLLE is applied as a dimensionality reduction technique is **0.92 to 0.96**. For all other dimensionality reduction techniques and when no dimensionality reduction technique is applied the Silhouette index ranges from **0.2 to 0.4**. So the bar graphs show dramatic improvement in silhouette index values when **HLLE** is applied as the dimensionality reduction technique as compared to other techniques or when no technique is applied, thereby showing improvement in quality of clustering. But the drawback of HLLE is that is **unable to predict the accurate number of clusters**. Its value of silhouette index remains constant for all values of partitions.

VI B. CHANGES IN DUNN INDEX

Next we consider changes in Dunn index. A higher value of Dunn index indicates better clustering results [5]. Figures 7 to 11 depict Dunn indices for different approaches. Horizontal axis shows different number of partitions and vertical axis depicts values of Dunn Index.

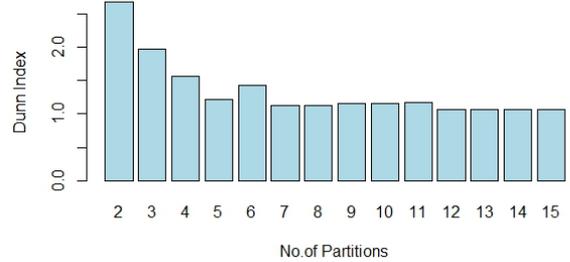


FIGURE NO.7 CHANGES IN DUNN INDEX WITH NO DIMENSIONALITY REDUCTION

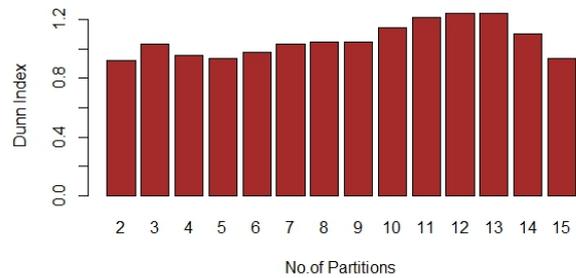


FIGURE NO.8 CHANGES IN DUNN INDEX WITH PCA AS DIMENSIONALITY REDUCTION TECHNIQUE

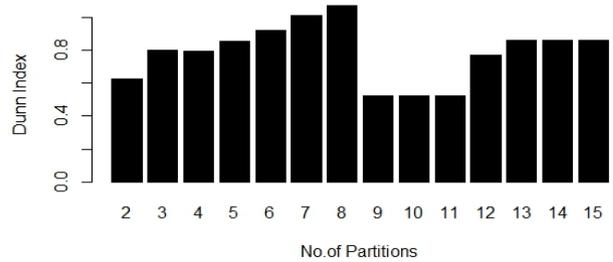


FIGURE NO.9 CHANGES IN DUNN INDEX WITH CMDS AS DIMENSIONALITY REDUCTION TECHNIQUE

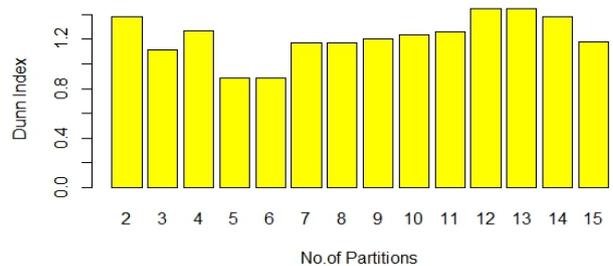


FIGURE NO.10 CHANGES IN DUNN INDEX WITH ISOMAP AS DIMENSIONALITY REDUCTION TECHNIQUE

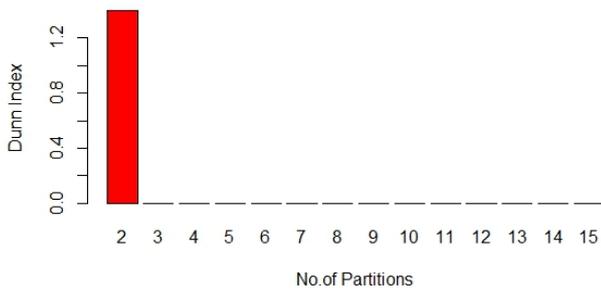


FIGURE NO.11 CHANGES IN DUNN INDEX WITH HLLE AS DIMENSIONALITY REDUCTION TECHNIQUE

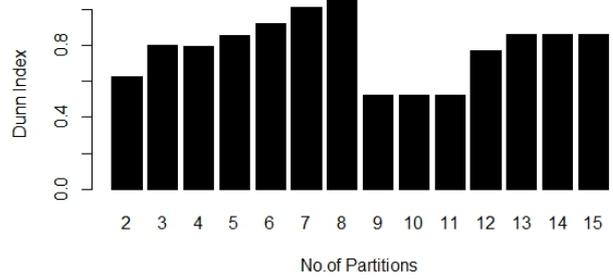


FIGURE NO. 14. CHANGES IN DAVIES-BOULDIN INDEX WHEN CMDS IS EMPLOYED

It is evident from figure 6 to figure 11 that Dunn Index values range from 0 to 2.8 for different dimensionality reduction techniques (the values are highest when no dimensionality reduction technique is applied). **So according to dunn index values, dimensionality reduction techniques don't improve performance of hierarchical clustering algorithm.**

VI C. CHANGES IN DAVIES - BOULDIN INDEX

Next index considered is Davies-Bouldin index. The smaller the value of this index, the better the clustering results [4]. Figures 12- 16 depict show variation in values of Davies-Bouldin index for different values of partitions.

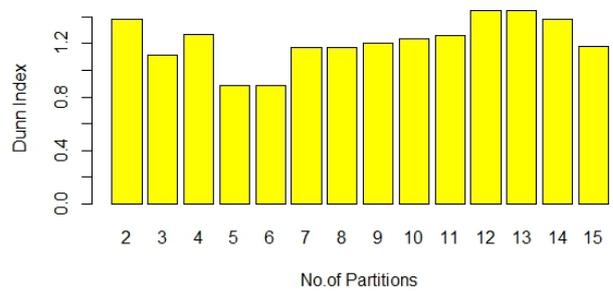


FIGURE NO. 15. CHANGES IN DAVIES-BOULDIN INDEX WHEN ISOMAP IS EMPLOYED

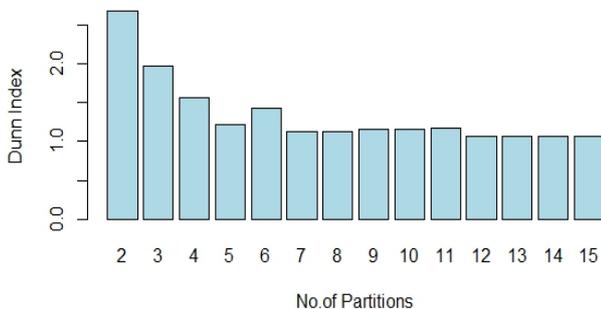


FIGURE NO. 12. CHANGES IN DAVIES-BOULDIN INDEX WHEN NO DIMENSIONALITY REDUCTION TECHNIQUE IS EMPLOYED

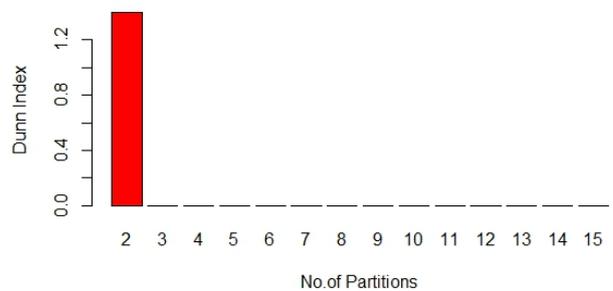


FIGURE NO. 16. CHANGES IN DAVIES-BOULDIN INDEX WHEN HLLE IS EMPLOYED

The figures 12 to 16 show that values of Davies-Bouldin Index approaches a **lower value** for correct number of clusters (The exception being FIGURE 14 where Davies-Bouldin index approaches lowest value for inaccurate number of clusters). But the variation in Davies-Bouldin indices is not much and so nothing can be concluded about efficacy of dimensionality reduction techniques.

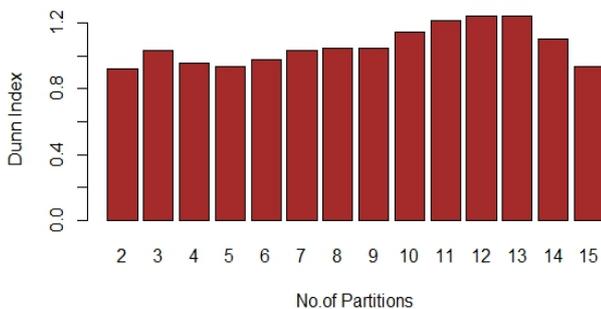


FIGURE NO.13. CHANGES IN DAVIES-BOULDIN INDEX WHEN PRINCIPAL COMPONENT ANALYSIS IS EMPLOYED

VI D. CHANGES IN CALINSKI-HARABASZ INDEX

Next we consider changes in Calinski-Harabasz Index. A **higher value of Calinski-Harabasz Index indicates better clustering results** [6]. Figures 17 to 21 depict the results.

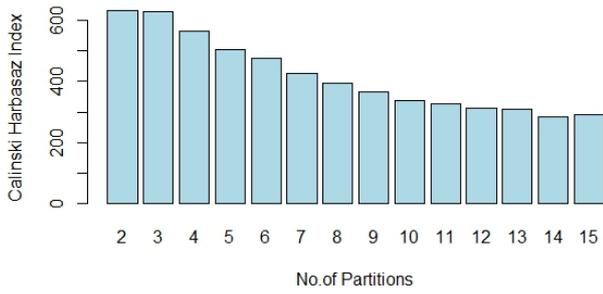


FIGURE NO.17. CHANGES IN CALINSKI HARBASAZ INDEX WHEN NO DIMENSIONALITY REDUCTION IS EMPLOYED

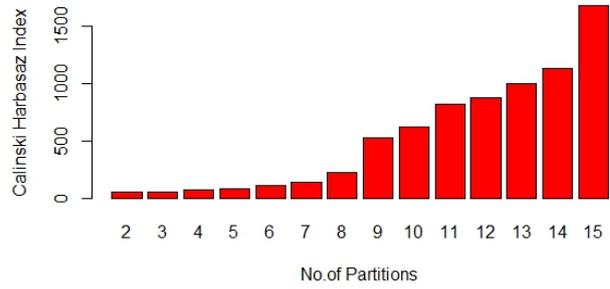


FIGURE NO.21. CHANGES IN CALINSKI HARBASAZ INDEX WHEN HLLC IS EMPLOYED

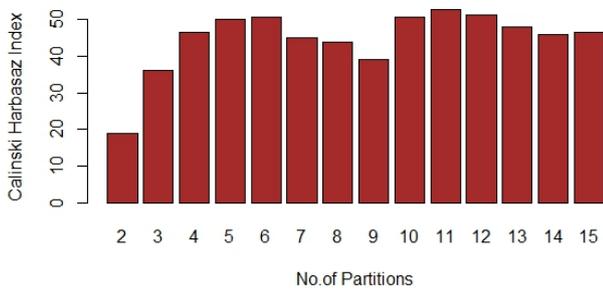


FIGURE NO.18. CHANGES IN CALINSKI HARBASAZ INDEX WHEN PCA IS EMPLOYED

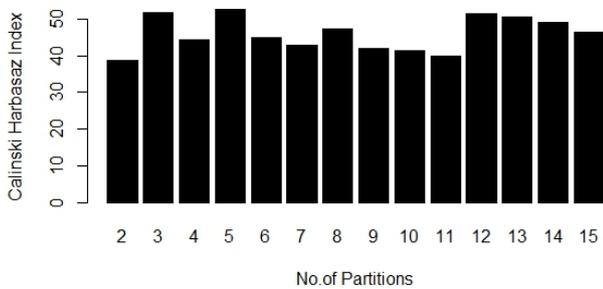


FIGURE NO.19. CHANGES IN CALINSKI HARBASAZ INDEX WHEN CMDS IS EMPLOYED

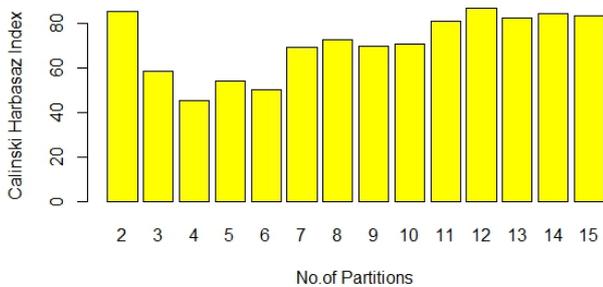


FIGURE NO.20. CHANGES IN CALINSKI HARBASAZ INDEX WHEN ISOMAP IS EMPLOYED

Figures 17 to 20 are inconclusive. The range of values for Calinski-Harbasaz (CH) Index remains the same from 50 to 100 (except in case of FIGURE 17 where the values range from 650 to 320). In some cases the Index values decrease for accurate number of clusters instead of increasing. But figure number 21 stands out from the rest. First of all the range of values are from 50 to 1100, 1100 being the value for number of partitions equal to 15 and 50 for number of partitions equal to 2. **So the CH Index is accurately predicting the number of partitions in the Libras Movement database.** Also the jump in the range of values (38 to 1673) indicate a corresponding jump in the quality of clustering. This indicates that for Libras data base with 90 attributes and 15 classes, **application of HLLC improves clustering.**

VII. AN IMPROVED HIERARCHAL CLUSTERING ALGORITHM

Based on above result the following figure 22 depicts an optimized data clustering HIERARCHAL DATA CLUSTERING algorithm.

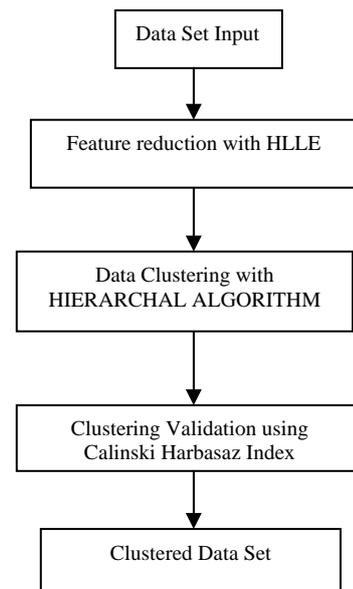


FIGURE NO.22. AN OPTIMIZED DATA CLUSTERING ALGORITHM

As it is clear from the above figure that our optimized HIERARACHAL DATA CLUSTERING algorithm uses **HLE** for dimensionality reduction and **CALINSKI HARBASAZ INDEX** for clustering validation.

VIII. CONCLUSIONS

In this paper different techniques of dimensionality reduction in conjunction with HIERARACHAL CLUSTERING algorithm are applied on Libras Movement database. To detect their effectiveness, four clustering validity indices are used. From the results obtained it can be concluded that **HLE** is a better dimensionality reduction technique than PCA, CMDS and ISOMAP for improvement of clustering results. Also **Calinski-Harbasaz** Index outperforms Dunn Index, Davies Bouldin Index and Silhouette Index for validating data clustering.

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